Clustering and PCA

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Datamining and Machine Learning

# Clustering

Clustering can be applied to data using the given *agglom*.*c* and *k*-*means*.*c* executable files. *Agglom*.*c* gives us a set of initial centroids that can be used for -means clustering to locally optimize those centroids. Additionally, the distortion for the given set of centroids relative to data are also outputted. Using the command prompt, inside the lab2-2021 directory, we can use the format agglom <dataFile> <centFile> <numCent> and k-means <dataFile> <centFile> <opFile> <numIter> to execute *agglom*.*c* and *k*-*means*.*c*, respectively.

## Distortion for Different Values of Initial Centroids

For one to ten initial centroids , we executed : agglom lab2Data lab2\_1C 1, until : agglom lab2Data lab2\_10C 10. Having produced ten more files, nine iterations of -means clustering was applied to them using the commands: k-means lab2Data lab2\_1C lab2\_1op 9, , k-means lab2Data lab2\_10C lab2\_10op 9. The first and last result of the distortion is shown in Fig. 1.

Graphical user interface, application, table

Description automatically generated

*(a)*

*(b)*

Fig. 1. distortion values for (a) K=1 and (b) K=10 initial centroids

The nine numbers appearing in Fig. 1, as well as every other output file, are the distortion values of the data after every iteration, when the centroid(s) are optimized and moved around. It can also be seen that after every iteration, the distortion value will decrease until it cannot decrease anymore. As for when , the distortion value stop decreasing after the second iteration because there is only one centroid, and after the second iteration, the algorithm was not able to locate a better location for the centroid to be in. But for , there are ten centroids being optimized and therefore, even subtle changes in one centroid might change the distortion values of the data.

Chart, line chart

Description automatically generatedTable 1: Final distortion values for K initial centroids

Fig. 2. Plotted final distortion values for K initial centroids

|  |  |
| --- | --- |
| initial centroids | Distortion[8] |
| 1 | 732439.6 |
| 2 | 317257.2 |
| 3 | 78126.7 |
| 4 | 32335.8 |
| 5 | 13455.1 |
| 6 | 5021.8 |
| 7 | 4581.7 |
| 8 | 3987.8 |
| 9 | 3529.1 |
| 10 | 3104.8 |

Table 1 and Fig, 2 shows the final distortion values after nine iterations as the initial centroid increases. With there being more centroids to cover a lot more spaces in the data, the distances between each data point to the closest centroid becomes smaller, therefore decreasing the distortion. But the huge decrease in distortion is mainly due to the centroids covering all the important groups and discovering the structure of the data.

From Fig. 2, it can be deduced roughly that there are around five to six groups of data rather than just being one big group. This is because even after increasing the initial centroids from six to seven, or eight, or nine, the amount of distortion starts to decrease smoothly, supposedly saying that the centroids have found the centre of the different groups. At low initial centroids, the distortion values are very big because the groups are probably far apart, and some centroids might even be in between two or three groups at once.

# Principal Component Analysis (PCA)

MATLAB was used to apply PCA to the data. The data was loaded using the line X = load('lab2Data-matlab');. To do PCA, we first require the covariance matrix of the data, which can be obtained using the line C = cov(X);. The result of the covariance matrix is

It is hard to deduce much about the data using the covariance matrix , so to get more information on the structure of the data we can use eigenvalue decomposition on the covariance matrix using the line [U,D] = eig(C). The results were eigenvectors and eigenvalues .

The eigenvectors tells us the rotation of the matrix and transforms the data so that it becomes the new matrix , which is our eigenvalues. While the eigenvalues from tells us that most of the variation of the data is contained in the new 5th dimension. And the least variation is in the 1st dimension, which could just be noise. The first three dimensions show negligible variations along their eigenvectors so it might be better to ignore them.

# Conclusion

-means clustering is very useful for finding groups of data that is unlabelled. By changing the values of the initial centroids, it is possible to find roughly how many groups are in the data by comparing the different distortion values. After increasing the initial centroids, if the distortion values are decreasing only by small amount, it means that the centroids have covered most of the data points, thus showing the structure and groups of the data.

On the other hand, PCA increases the interpretability of the data and minimizes information loss. The values of the eigenvectors and eigenvalues after finding the covariance matrix is crucial in determining where most of the data is located and simplifies very high-dimensional data.